

# Modelling Contagion in Financial Networks

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and

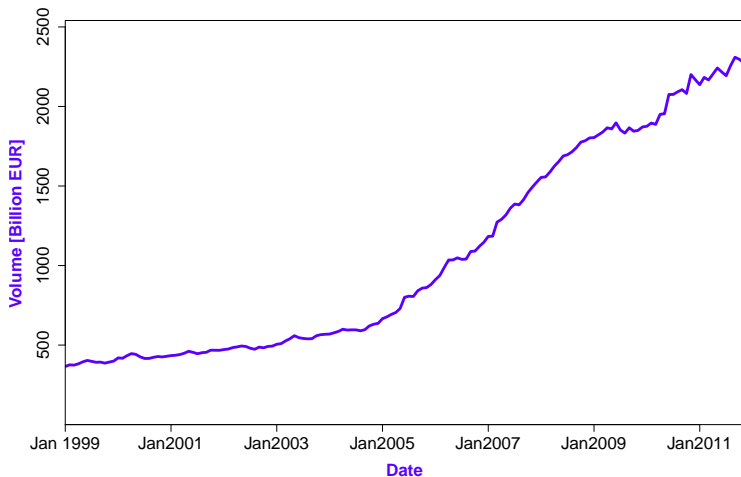
Graduate School "Foundations of Global Financial Markets"  
Friedrich-Schiller-Universität Jena

Cambridge University, Judge Business School, Center for Risk Studies  
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- The financial system has become increasingly **interconnected** and **complex**
- Supervision of individual financial institutions insufficient
  - ⇒ **Network structure** of interconnections matters
- Systemic risk takes various forms and is highly dynamic
  - ⇒ Better understanding needed to safeguard **financial stability**

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- This talk: **agent-based models** and **network theory** to address these questions

# The interconnectedness of the Financial System Increased



**Figure:** Deposits of euro area MFIs vs. other euro area MFIs, not seasonally adjusted.

Source: ECB

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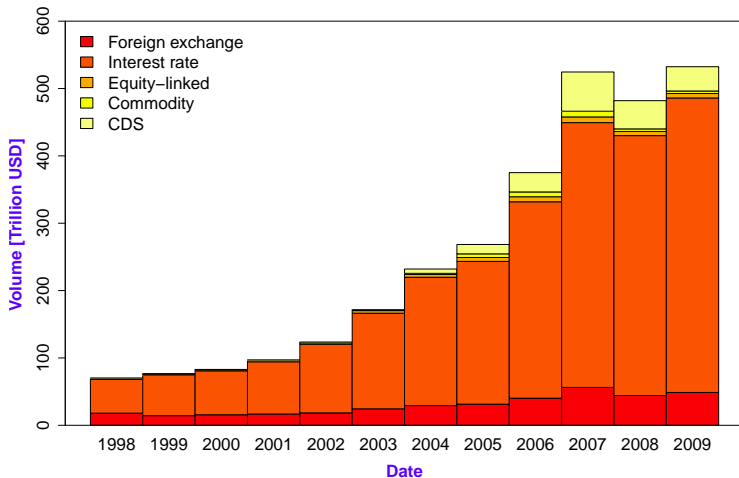


Figure: Global over-the-counter derivatives markets, notional amounts of contracts outstanding. Source: IMF

# Indirect linkages amplify the risk of fire-sales

## U.S. Mortgage-Related Securities Issuance

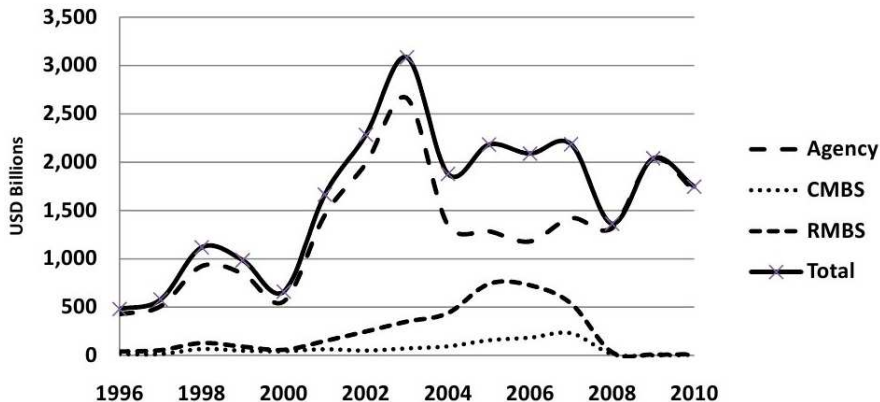
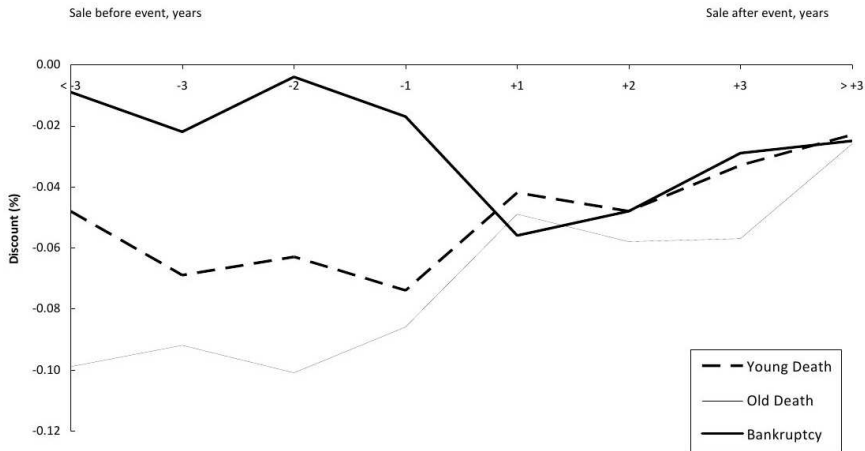


Figure: U.S. Mortgage-Related Securities Issuance. Source: Gorton and Metrick (2010)

# Indirect linkages amplify the risk of fire-sales



**Figure:** Forced Sales Discounts and Time Between Sale and Event. Source: Campbell, Giglio and Pathak (2012)

# Indirect linkages amplify the risk of fire-sales

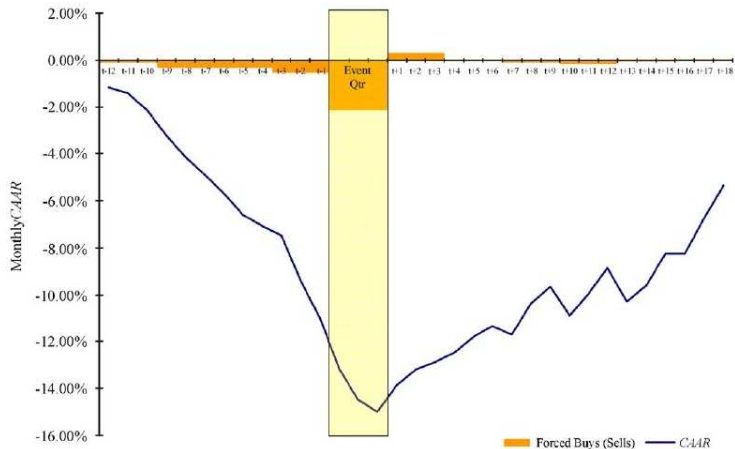


Figure: Cumulative average abnormal returns around mutual fund fire sales. Source: Coval and Stafford (2007)



# Do We Need Yet Another Paper?

## Literature on Financial Networks

- Allen and Gale (2000), Freixas et al. (2000)
- Haldane and May (2011), Gai et al. (2011), Gai and Kapadia (2008)
- Becher et al. (2008), Gabrieli (2011), Chang et al. (2008), Brink and Georg (2011), Markose et al. (2010)

## Literature on Fire-sales

- Shleifer and Vishny (1992): specialised asset holders are simultaneously in distress and sell to non-specialists
- Allen and Gale (1994): endogenous market participation

## Literature on Multi-Agent Models:

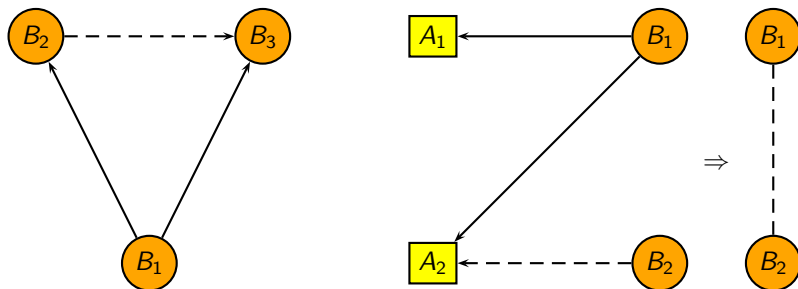
- Iori et al. (2006), Nier et al. (2007)
- **However:** risk-free investments, no central bank, mechanistic agent behaviour, “fine-tuning”

# What is Systemic Risk?

## Definition by impact

- FSB definition: *“a risk of disruption to financial services that is (i) caused by an impairment of all or parts of the financial system and (ii) has the potential to have serious negative consequences for the real economy.”*

## Definition by cause

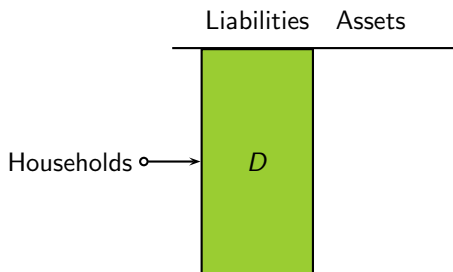


**Figure:** Left: direct connections (counterparty risk, contagion). Right: indirect connections (common shocks, fire-sales).

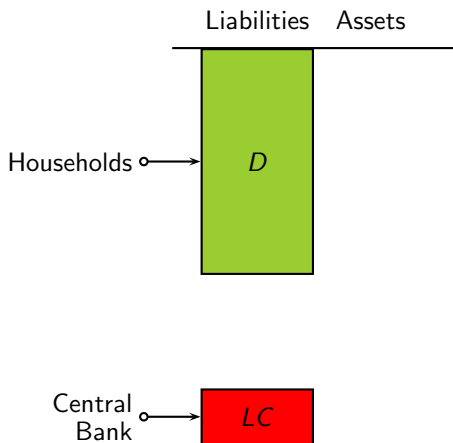
# Focus of this Paper

- Complete dry-up of interbank markets in September 2008, central banks were forced to unprecedented non-standard measures  
⇒ **Q1: Can central banks stabilize interbank markets?**
- Systemic risk requires macroprudential oversight in addition to microprudential supervision  
⇒ **Q2: What are robust network structures?**
- Different forms of systemic risk can act differently on the financial system  
⇒ **Q3: What are the optimal policy responses?**

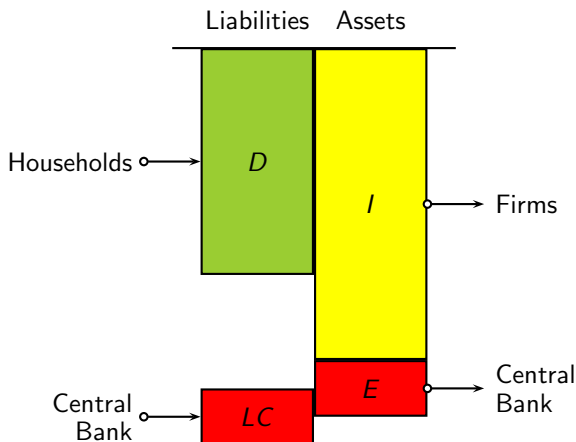
# Microfoundations of Banks Determine Model



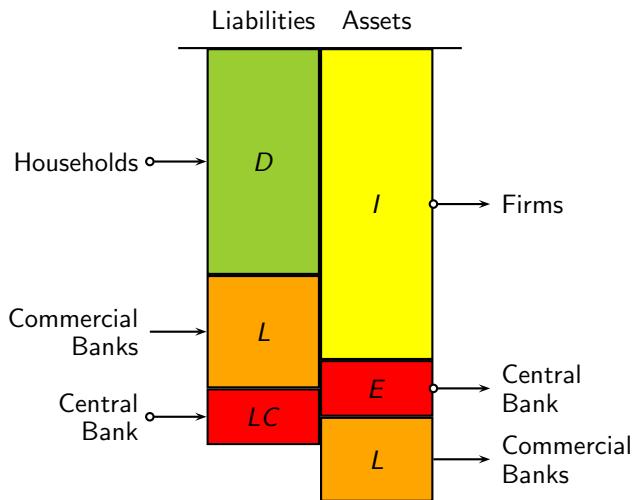
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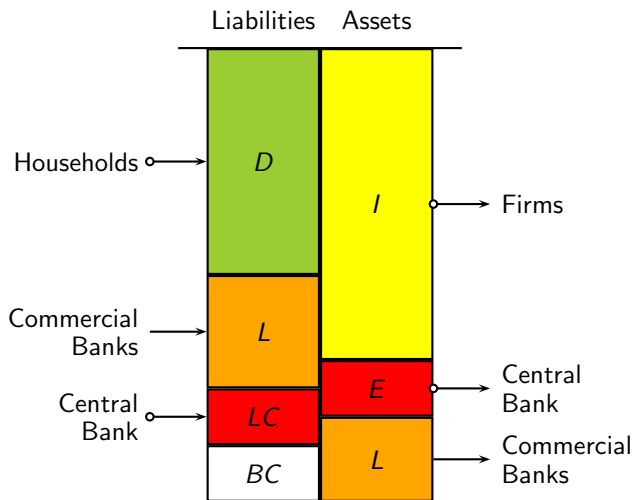
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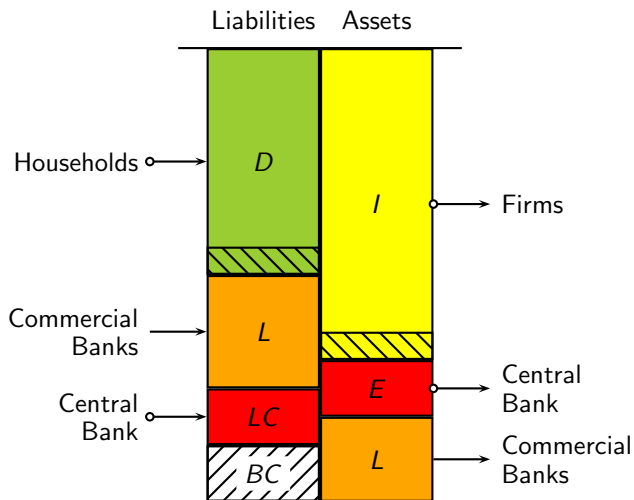


# Microfoundations of Banks Determine Model





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# Agent Behaviour has to be Motivated

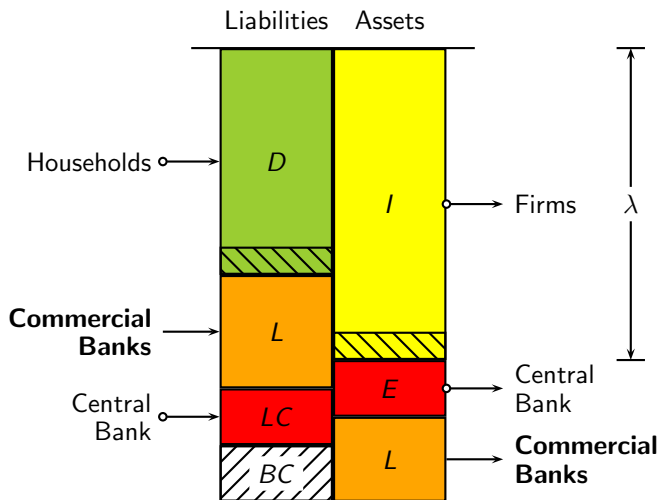
- Banks optimize their **portfolio structure and -volume** according to CRRA preferences

$$u = \frac{1}{1-\theta} \left( V(1 + \lambda\mu - \frac{1}{2}\theta\lambda^2\sigma^2) \right)^{(1-\theta)}$$

where  $\theta$  is risk-aversion parameter

- **Update algorithm** for  $k = 1, \dots, N$  banks and  $t = 1, \dots, \tau$  update steps:
  - 1 Obtain returns on investments, pay interest on deposits
  - 2 Deposit in- and out-flows, required reserves
  - 3 Settle interbank loans
  - 4 Determine new investment level
  - 5 Settle liquidity position
  - 6 Pay dividends

# Microfoundations of Banks Determine Model



# Interbank Loans Form a Network Structure

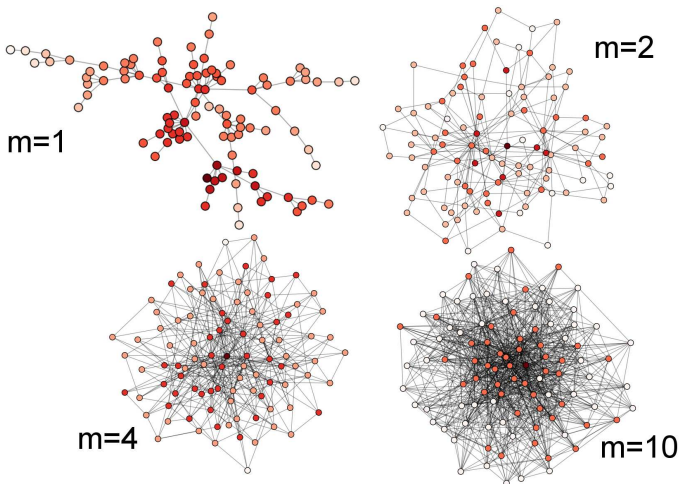


Figure: Different scale free networks

# Model Parameters

Sektor	Parameter
Households	deposit fluctuations $\gamma$
Firms	credit success probability $p_f$ , <b>realized credit return</b> $(\rho_f^+, \rho_f^-)$
Commercial banks	deposit interest rate $r^d$ , dividend level $\beta^k$ , expected credit success probability $p_b$ , expected credit return $(\rho_b^+, \rho_b^-)$ , risk aversion parameter $\theta$
Central bank	main refinancing rate $r^b$ , minimum reserve requirement $r$ , <b>quality of securities</b> $\alpha^k$

## Network parameters

number of banks  $N$ , **level of interbank connections** `connLevel`

## Simulation parameters

number of update steps  $\tau$ , number of simulations `numSimulations`

# Central Bank Liquidity Stabilizes in the Short-Run...

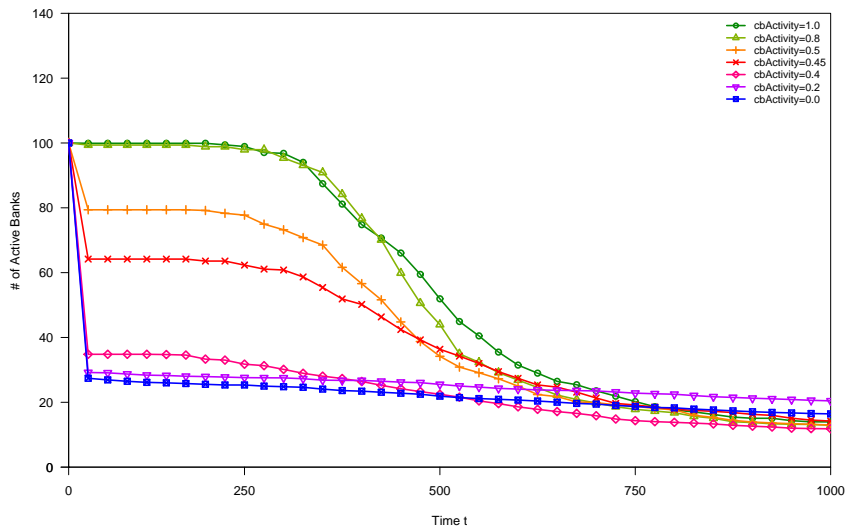
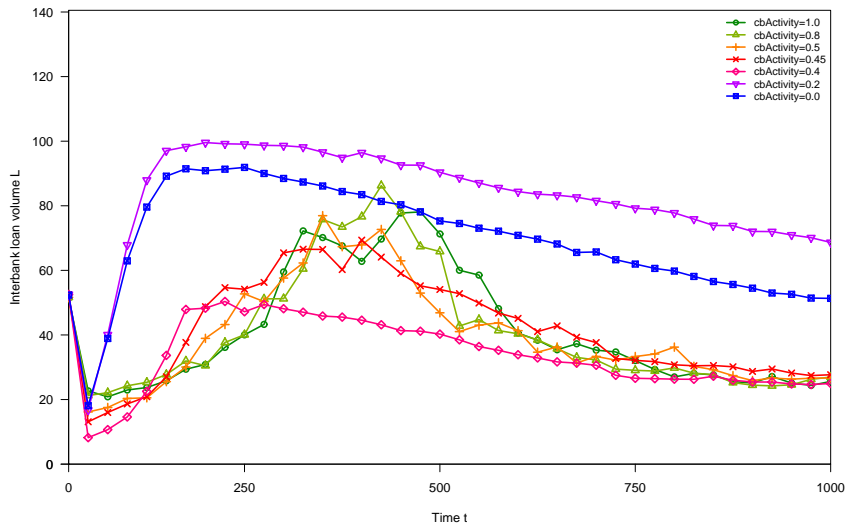


Figure: The effect of central bank activity  $\alpha^k$  on financial stability in a crisis scenario ( $\rho_f^+ = 0.09$ ,  $\rho_f^- = -0.08$ )

# ...but the Effect is Non-Monotonic



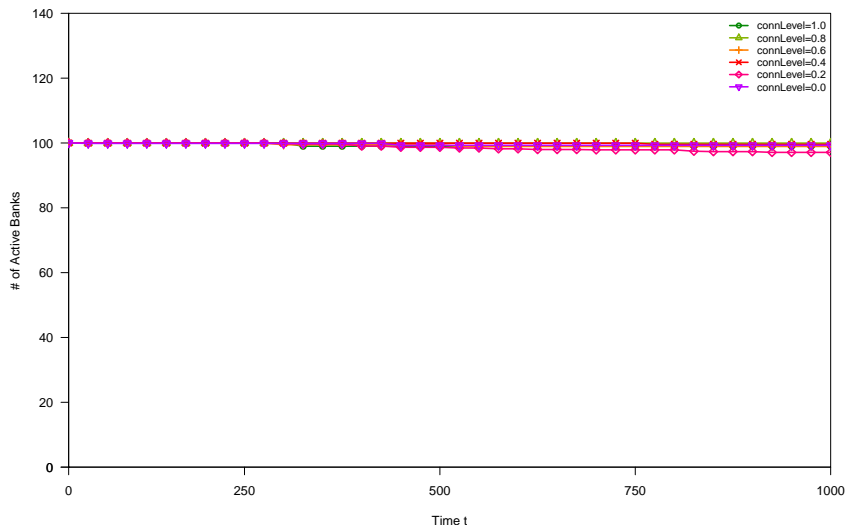
**Figure:** The effect of central bank activity  $\alpha^k$  on interbank liquidity in a crisis scenario ( $\rho_f^+ = 0.09, \rho_f^- = -0.08$ )

## Lesson 1:

- Central bank liquidity provision has **non-linear** effect on financial stability
  - ⇒ Close threshold value, small changes have significant impact
  - ⇒ Away from threshold value, even large changes can be ineffective
- Stabilizing effect in the **short-run** only
- Abundant central bank liquidity **crowds out** interbank liquidity

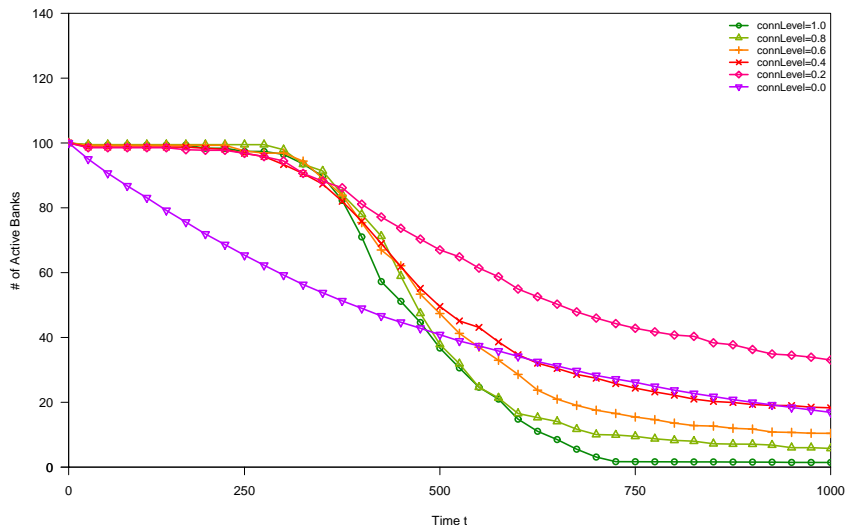


# Some Network Structures are More Resilient Than Others



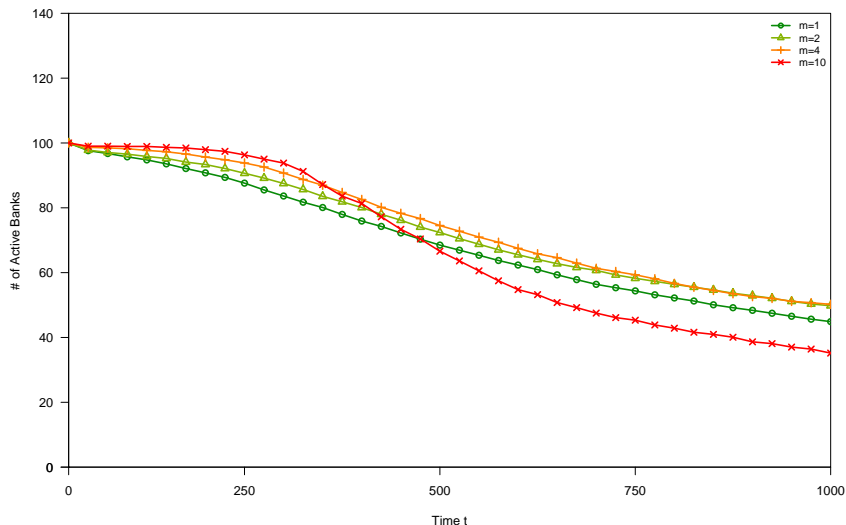
**Figure:** The impact of the network topology on financial stability in a normal scenario ( $\rho_f^+ = 0.09, \rho_f^- = -0.05$ ) in a random network.

# Some Network Structures are More Resilient Than Others



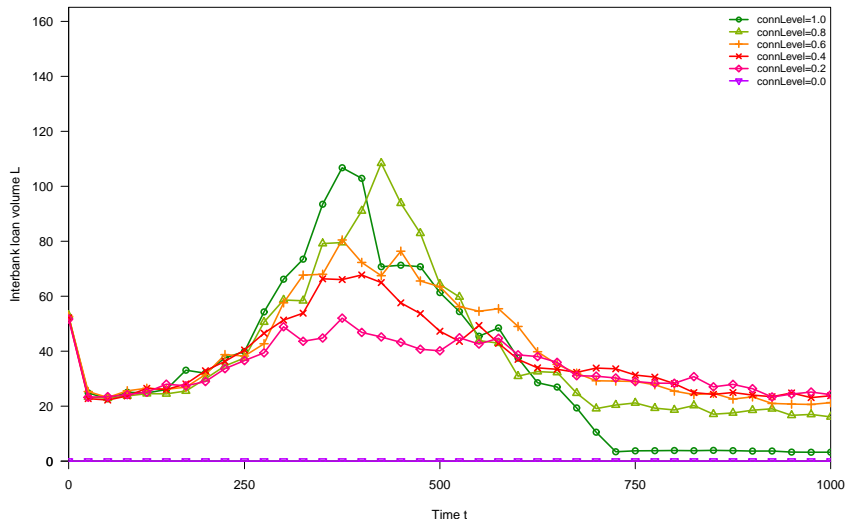
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**Figure:** The impact of the network topology on financial stability in a crisis scenario ( $\rho_f^+ = 0.09, \rho_f^- = -0.08$ ) in a BA network

# Some Network Structures are More Resilient Than Others



**Figure:** The impact of the network topology on interbank liquidity in a crisis scenario ( $\rho_f^+ = 0.09, \rho_f^- = -0.08$ ) in a random network

## Lesson 2:

- Network **structure matters** in crises
- Relationship between financial stability and interconnectedness in random networks is **non-monotonic**
- Scale-free networks tend to be **more stable** than random networks
- Interbank networks are **robust-yet-fragile**  
⇒ Size of endogenous fluctuations matter

# Different Forms of Systemic Risk Require Different Answers

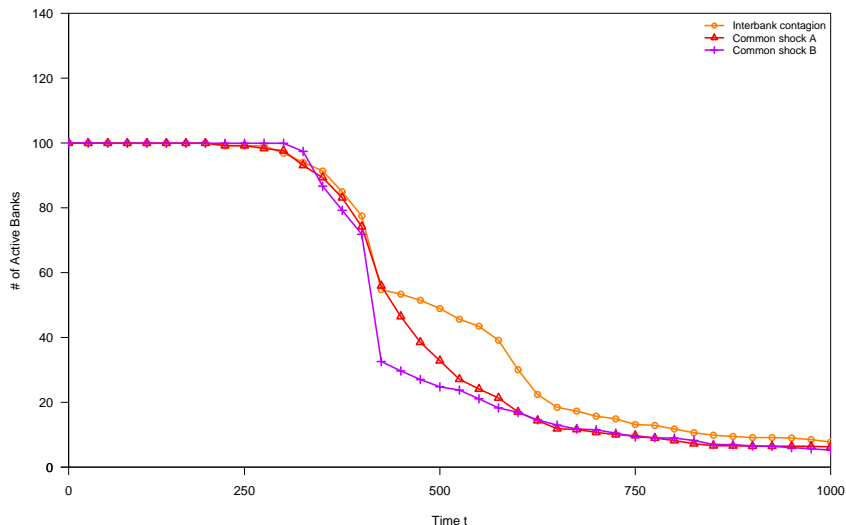
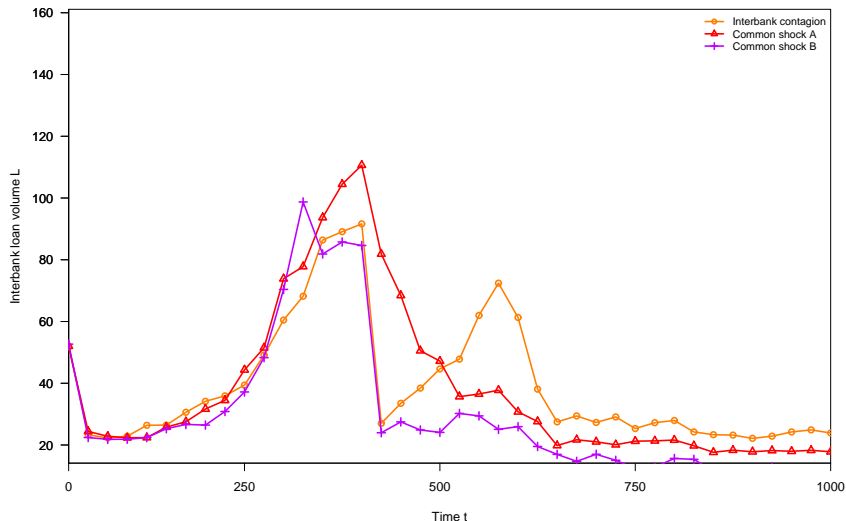


Figure: The impact of different forms of systemic risk on financial stability in a crisis scenario ( $\rho_f^+ = 0.09, \rho_f^- = -0.08$ ) in a random network ( $\text{connLevel}=0.8$ )

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**Figure:** The impact of different forms of systemic risk on financial stability in a crisis scenario ( $\rho_f^+ = 0.09, \rho_f^- = -0.08$ ) in a random network ( $\text{connLevel}=0.8$ )

## Lesson 3:

- Common shocks can pose greater threat to financial stability
- Contagion mainly reduces **liquidity** available in the system
- Common shock mainly reduces **banking capital** and increases (relative) size of endogenous fluctuations
  - ⇒ Different optimal responses, for different forms of systemic risk
  - ⇒ Implications for financial Regulation



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**Thank you!**

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