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Locational-based Coupling of Electricity Markets: Benefits from Coordinating Unit Commitment & Balancing Markets

(EPRG Working Paper 1022 / Cambridge Working Paper in Economics 1044)

Harry van der Weijde | hweijde@feweb.vu.nl | EPRG & VU Amsterdam

Benjamin F. Hobbs | bhobbs@jhu.edu | EPRG, Johns Hopkins & California ISO

INFORMS Annual Meeting, 7-10 November 2010, Austin TX

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Overview

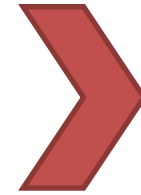
1. **What** are we estimating?
2. **How**?
 - a) Modelling framework
 - b) Numerical application
3. What are the **results** in a “base case”?
4. How do these results depend on various parameters (**sensitivity**) ?
5. What can we **conclude**?



1. What are we estimating?

Potential Benefits of LMP:

- Short-run improvements
 - within-country dispatch
 - international dispatch/trade
 - unit commitment
 - demand response
 - avoiding inc-dec-games
- Long-run improvements
 - siting of investment
 - mix of investment
 - less transmission investment needed



**This study
(in a simple
network
+ sensitivities)**



2a. How? Model framework

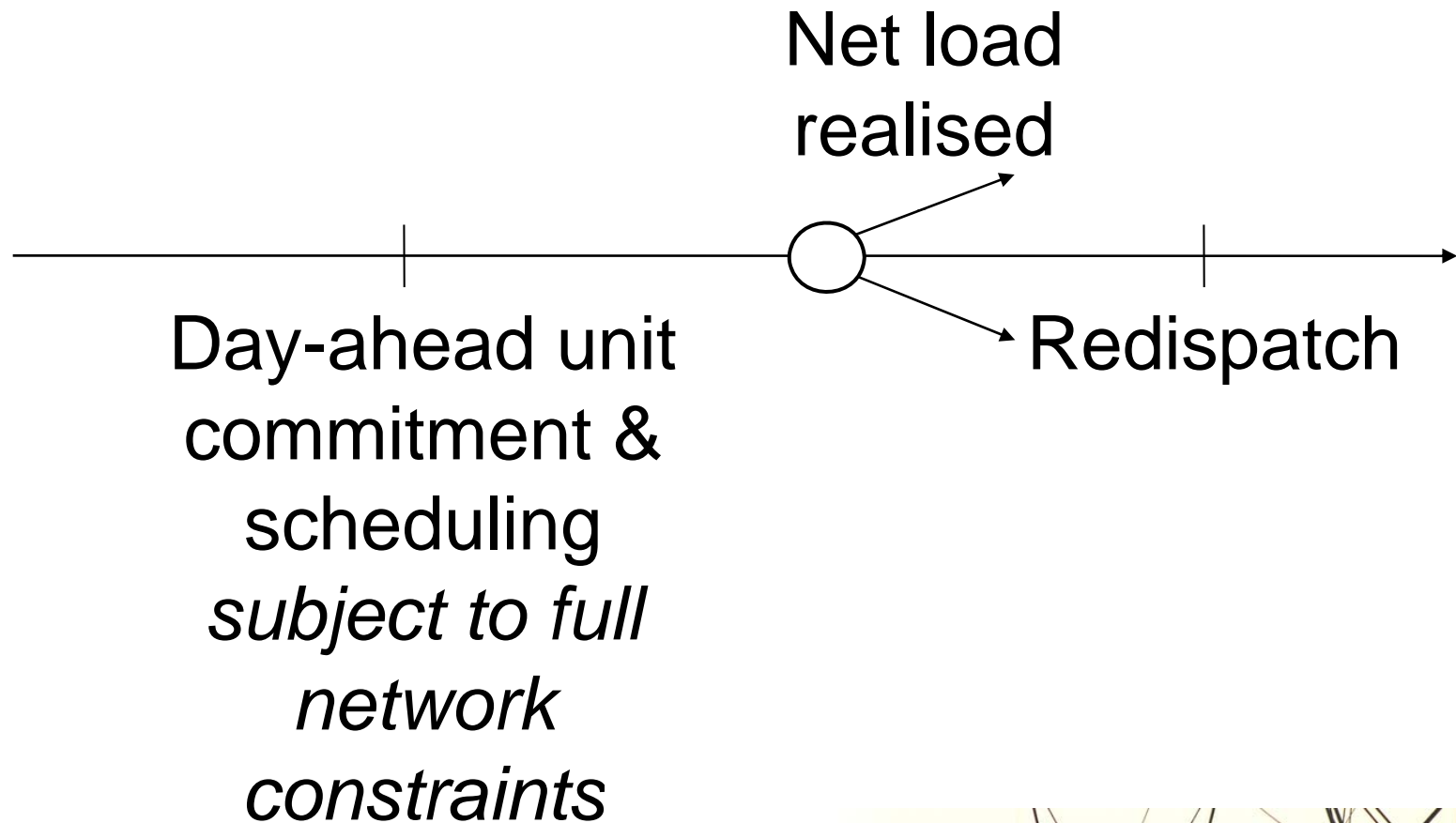
- **Three models** calculating expected cost (EC) of commitment & dispatch
 - 1) LMP: commit s.t. full network (*lowest cost!*)
 - 2) NTC-ID: commit s.t. NTC , followed by international redispatch
 - “Net Transfer Capability” = Total MW limit between countries
 - This is an approximation to true network constraints → cost increase
 - 3) NTC-NID: commit s.t. NTC, only domestic redispatch
- Calculate **unit commitment benefits**: $EC[NTC-ID] - EC[LMP]$

Quantified for two NTC cases:

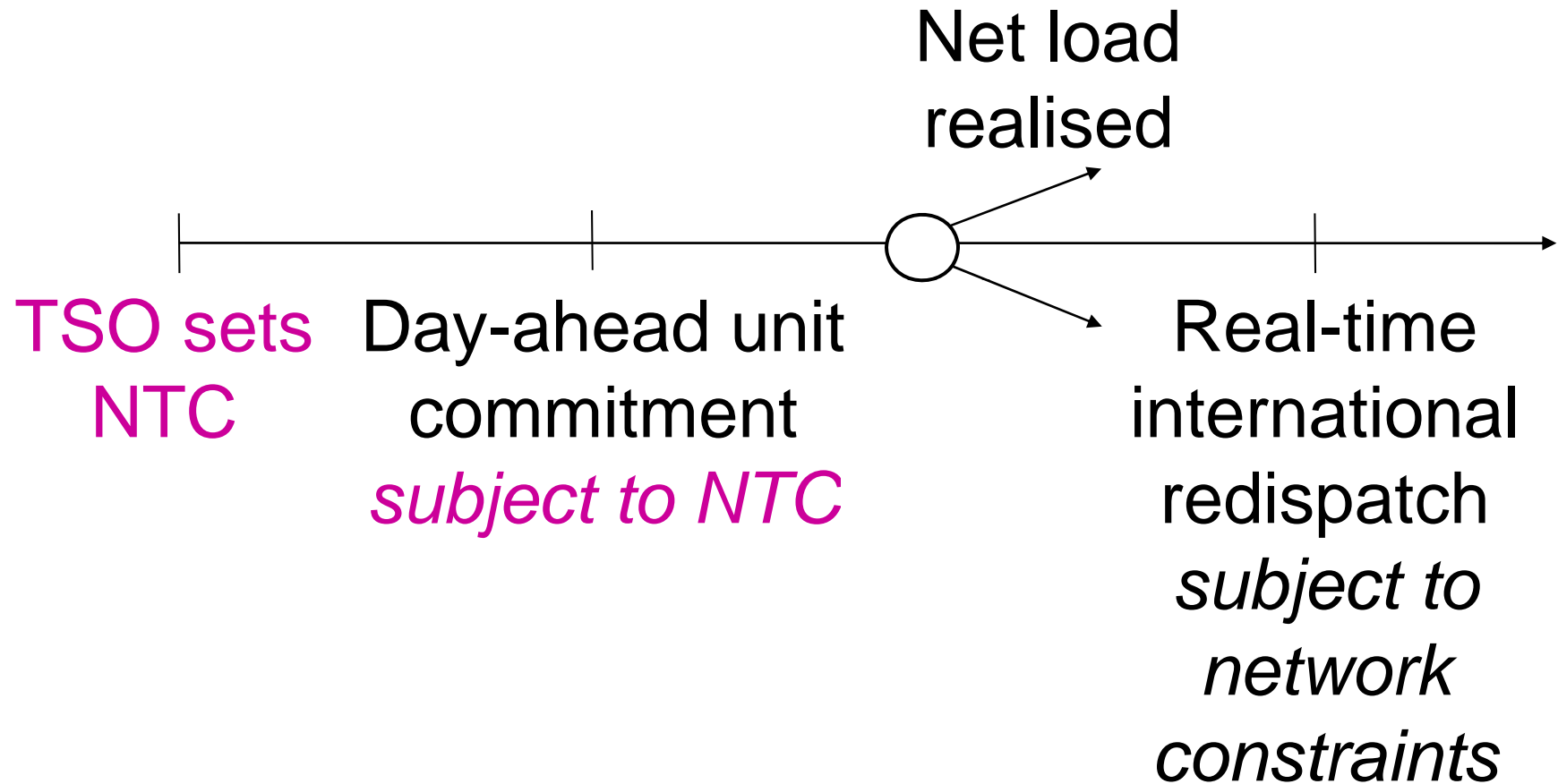
 - 1) Optimal NTC (minimize expected costs) → through search over NTCs
 - 2) Arbitrary (fixed) NTC
- Calculate **benefits of international redispatch**:
 $EC[NTC-NID] - EC[NTC-ID]$
- **Sensitivity** analysis to network parameters



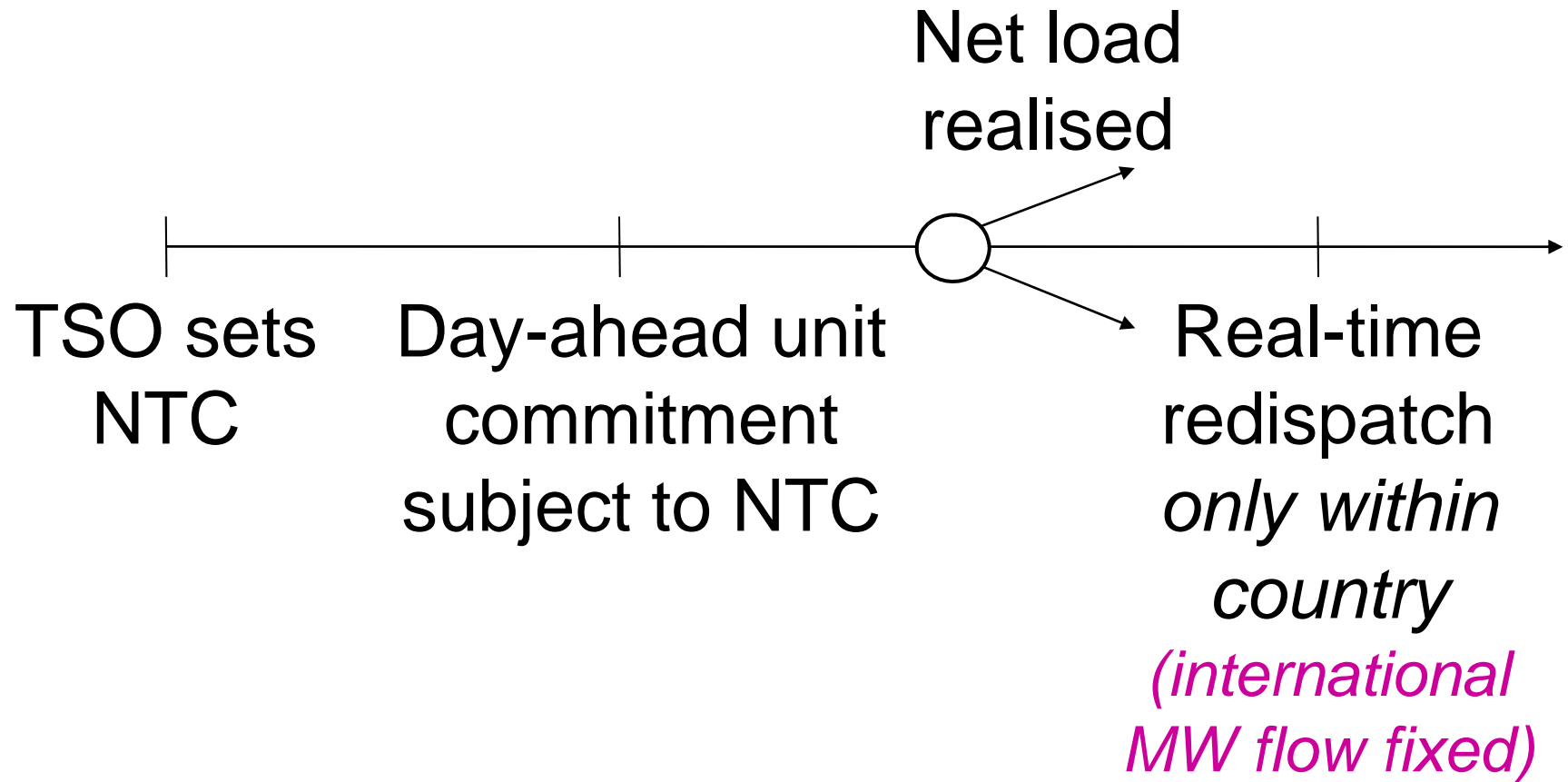
Model LMP



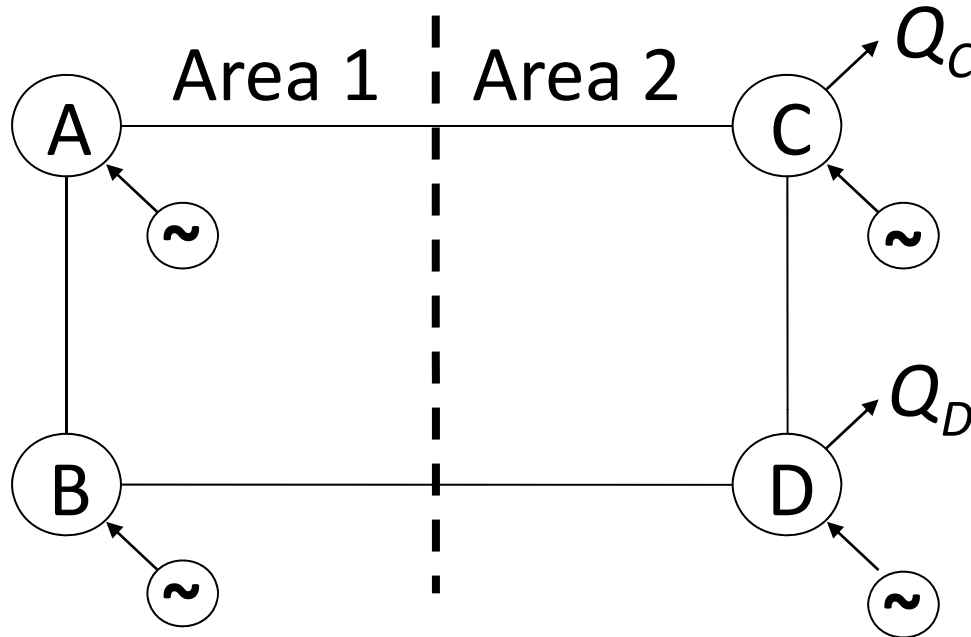
Model NTC-ID



Model NTC-NID



2b. How? Numerical application



Transmission: Equal reactance, line limits = 1000 MW

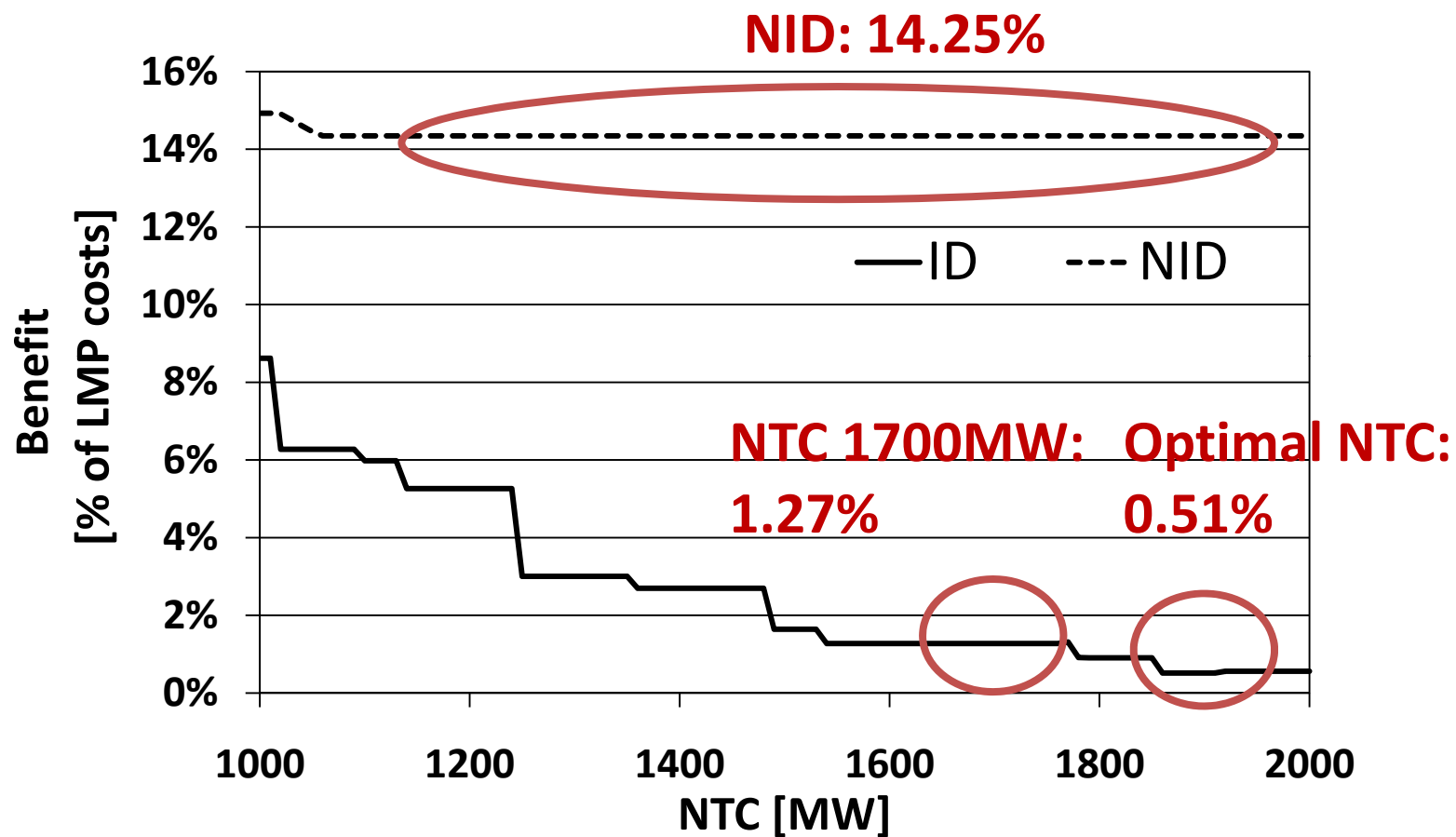
- **Hence: $1000 \text{ MW} \leq \text{NTC} \leq 2000 \text{ MW}$: search over this interval**

Generation: 12 generators (based on Bard, 1988)

- **Baseloaded plants ignored**
- Day-ahead unit commitment for 24 hours (grouped into 3 time periods)

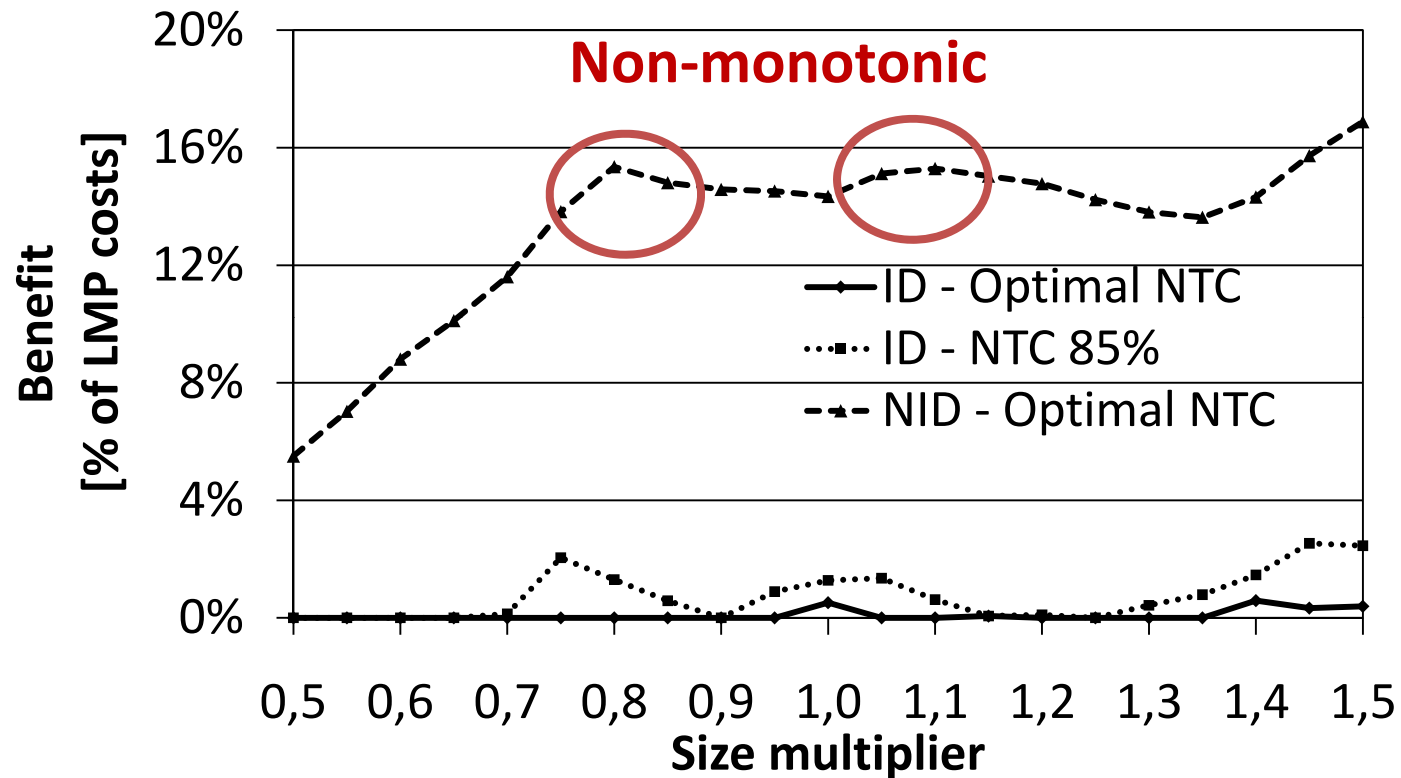


3. What are the results in a 'base case'?



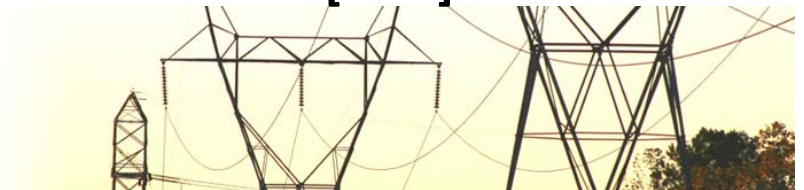
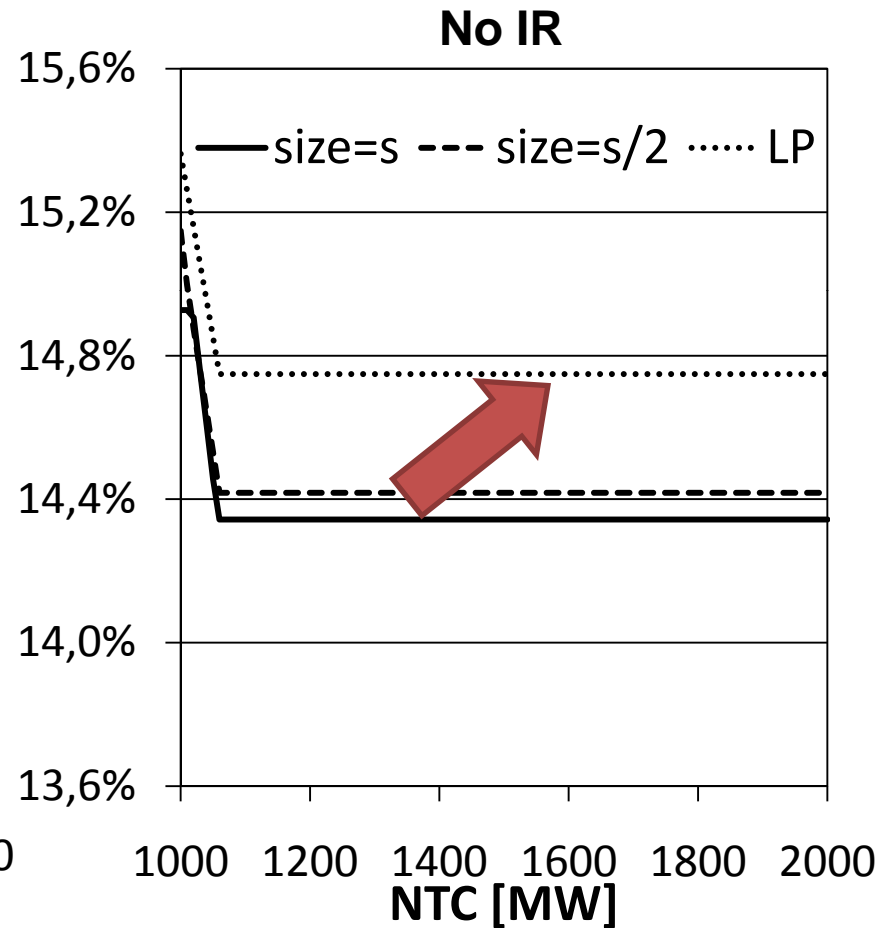
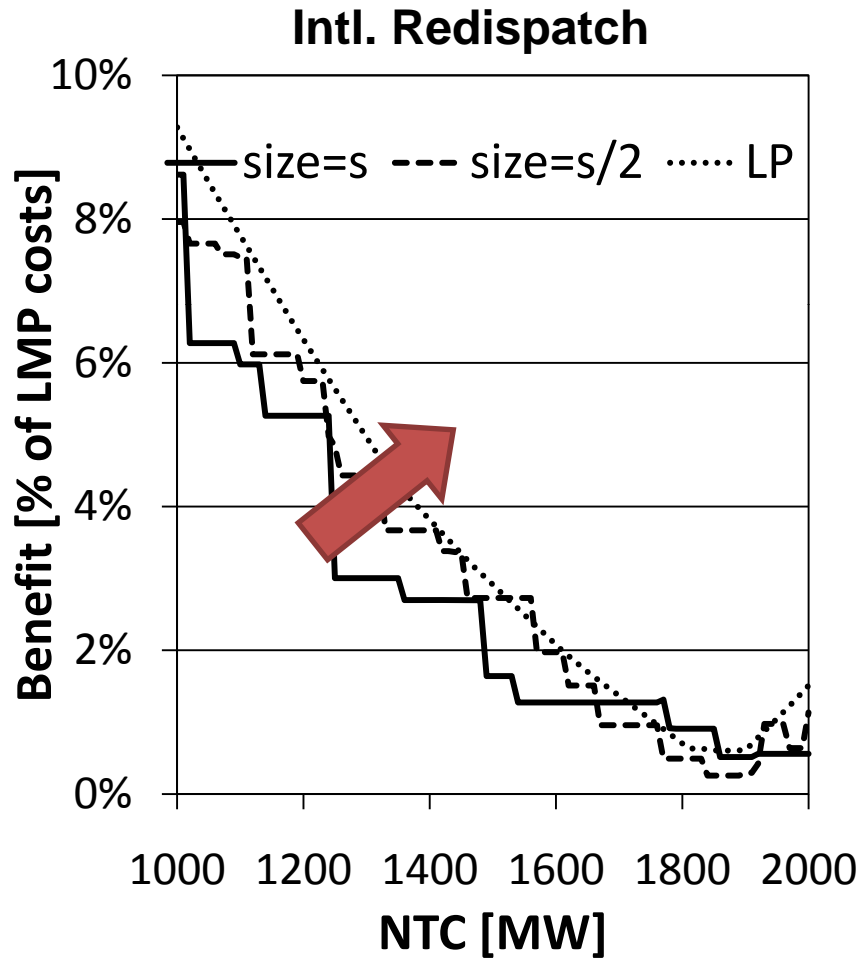
4. Sensitivity: generator size

(min run, max run, start-up costs, fixed costs multiplied)



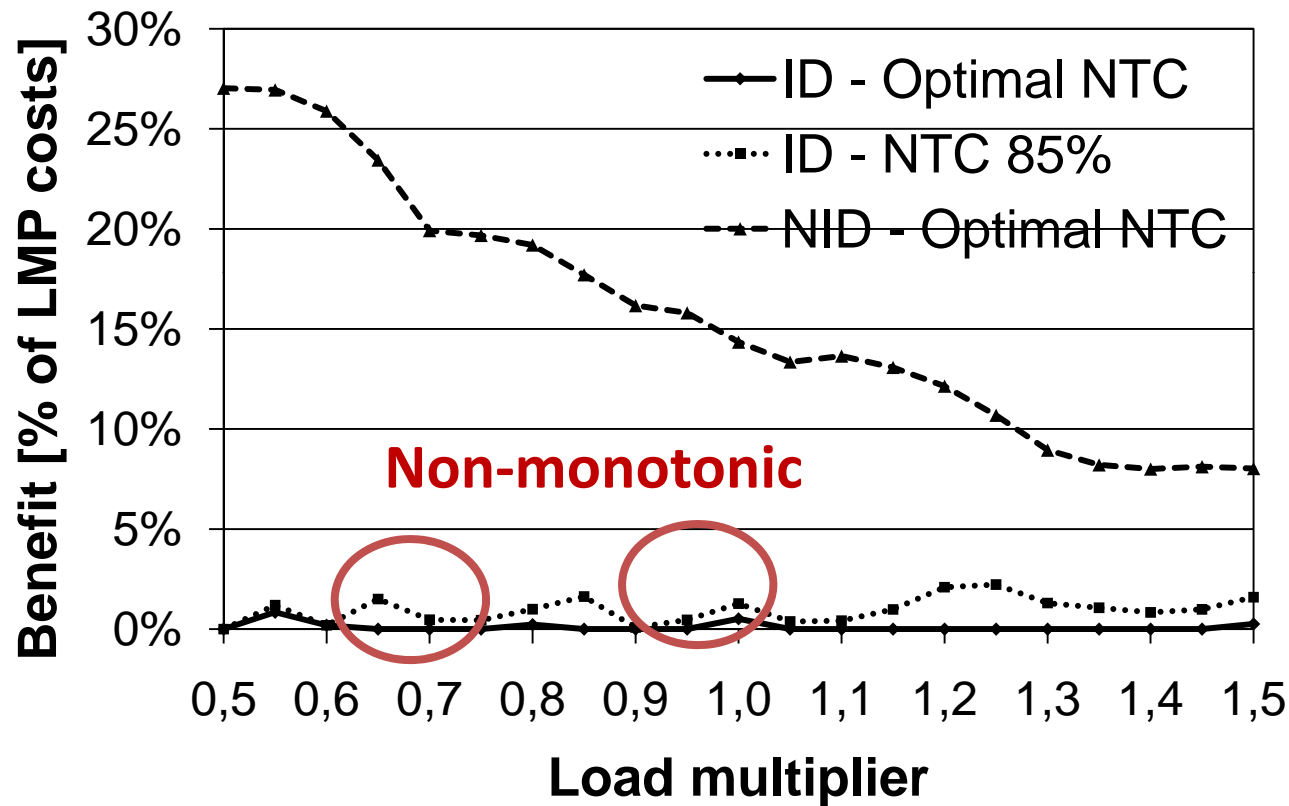
4. Sensitivity: generator lumpiness

Keeping aggregate system capacity constant



4. Sensitivity: Load levels

Load at all nodes scaled up & down



5. What can we conclude?

- LMP can significantly improve unit commitment decisions (saving 0-1% of fuel costs of non-baseload plants)
- Intl balancing can provide significant benefits even if unit commitment decisions consider only NTC constraints
- Magnitudes greatly depend on exact characteristics of the electricity market
- Cf. other studies
 - *0.1% Unit commitment benefits in EU* (R. Barth et al., Load-Flow Based Market Coupling with Large Scale Wind Power in Europe. 8th Workshop on Large-Scale Integration of Wind Power in Power Systems, 2009)
 - *0.38 €/MWh Intl. redispatch benefits in F-Be-NL-G example* (Oggioni & Smeers, Degrees of Coordination in Market Coupling and Counter-Trading, UCL, 2009)



5. What can we conclude?

- Intl Redispatch:

 - ↓ generator size, ↑ min run levels

 - ↑ load symmetry, ↑ load correlation

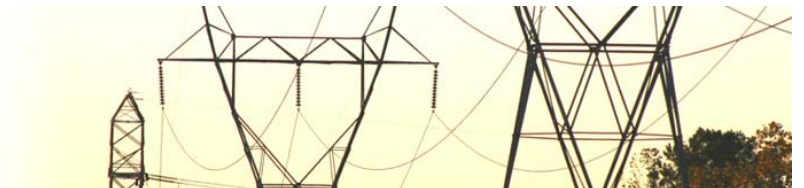
- NIR: ↓ generator size, ↑ min run levels

 - ↑ transmission capacity, ↓ load level

 - ↑ load symmetry ↑ load correlation

↑ benefits

- continuous approximations of binary commitment variables can significantly overstate UC benefits for small systems.





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Appendices



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UC model

$$\min_{\{s_{it}, z_{it}, p_{ijt}\}} \sum_{t \in T} \left[\sum_{i \in I} (SU_i s_{it} + H_t FC_i z_{it}) + \sum_{j \in J} PR_j H_t \sum_{i \in I} MC_i p_{ijt} \right]$$

s.t.

$$P_i^{\min} z_{it} \leq p_{ijt} \leq P_i^{\max} z_{it}$$

$$z_{it} - z_{i,t-1} \leq s_{it}$$

$$s_{it} \geq 0$$

$$\sum_{i \in I} p_{ijt} = \sum_{h \in H} Q_{hjt}$$

and for NTC:

$$\sum_{i \in I^A} p_{ijt} + \sum_{i \in I^B} p_{ijt} \leq NTC$$

and for LMP:

$$\sum_{h \in H} PTDF_{hk} \left(\sum_{i \in I^h} p_{ijt} - Q_{hjt} \right) \leq T_k$$



Dispatch model

$$\min_{\{\bar{p}_{ijt}, l_{jt}\}} \sum_t H_t \left(\sum_{i \in I} MC_i \bar{p}_{ijt} + l_{jt} CL \right)$$

s.t.:

$$P_i^{\min} z_{it}^* \leq \bar{p}_{ijt} \leq P_i^{\max} z_{it}^*$$

$$\sum_{i \in I} \bar{p}_{ijt} = \sum_{h \in H} Q_{hjt}$$

$$\sum_{h \in H} PTDF_{hk} \left(\sum_{i \in I^h} \bar{p}_{ijt} - Q_{hjt} \right) \leq T_k$$

and for NID:

$$\sum_{i \in I^A} \bar{p}_{ijt} + \sum_{i \in I^B} \bar{p}_{ijt} + l_{jt} = \sum_{i \in I^A} p_{ijt}^* + \sum_{i \in I^B} p_{ijt}^* \quad l_{jt} \geq 0$$



Benefit calculation

- Costs for each model:

$$E[TC] = \sum_{t \in T} \left[\sum_{i \in I} SU_i s_{it}^* + H_t FC_i z_{it}^* + \sum_{j \in J} PR_j H_t \sum_{i \in I} (MC_i \bar{p}_{ijt}^* + l_{jt} CL) \right]$$

- Benefit = $E[TC_{NTC}] - E[TC_{LMP}]$

